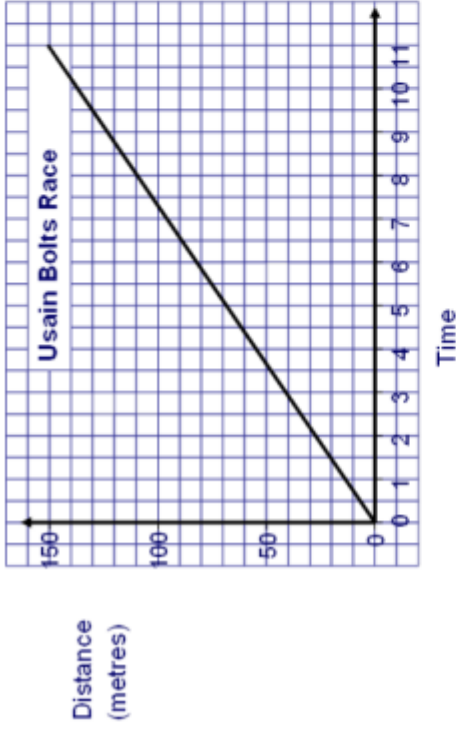




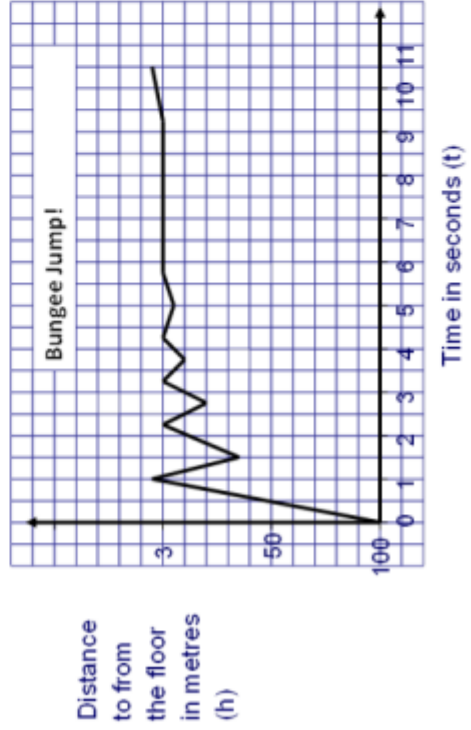
Topic/Skill	Definition/Tips	Example
1. Real Life Graphs	<p>Graphs that are supposed to model some real-life situation.</p> <p>The actual meaning of the values depends on the labels and units on each axis.</p> <p>The <b>gradient</b> might have a contextual meaning.</p> <p>The <b>y-intercept</b> might have a contextual meaning.</p> <p>The <b>area</b> under the graph might have a contextual meaning.</p>	<p>A graph showing the cost of hiring a ladder for various numbers of days.</p> <p>The gradient shows the cost per day. It costs £3/day to hire the ladder.</p> <p>The y-intercept shows the additional cost/deposit/fixed charge (something not linked to how long the ladder is hired for). The additional cost is £7.</p>
2. Conversion Graph	<p>A line graph to <b>convert one unit to another</b>.</p> <p>Can be used to convert units (e.g. miles and kilometres) or currencies (\$ and £)</p> <p>Find the value you know on one axis, read up/across to the conversion line and read the equivalent value from the other axis.</p>	<p>Conversion graph miles ↔ kilometres</p> <p><math>8\text{ km} = 5\text{ miles}</math></p>
3. Depth of Water in Containers	<p>Graphs can be used to show how the depth of water changes as different shaped containers are filled with water at a constant rate.</p>	



**Try These**

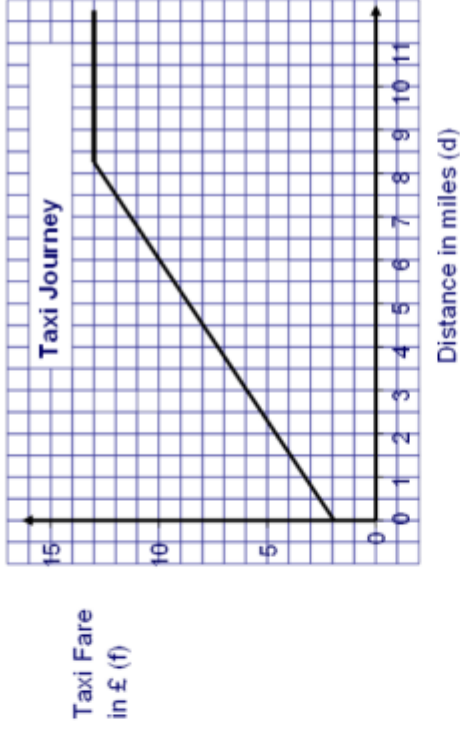


- How far has he run after 4.5 seconds?
- How long has it taken Usain to run 130 metres?
- How far has he run after 8 seconds?
- Why does the line go through the origin?



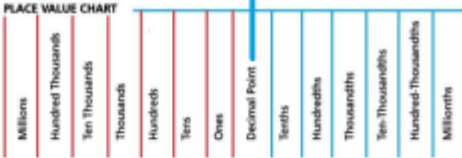
Distance to the floor in metres (h)

- How high is the bungee jump?
- Why does the graph zig zag?
- How long is the person falling for until they begin to bounce back up?
- Why does the person stop at 3 metres and not 0?
- How long is the person not bouncing but still upside down for?




- Why does the taxi fare not go through the origin?
- How much does it cost to travel 6 miles?
- How far can I travel if I only have £10 in my pocket?
- What does the journey cost after 9 miles? And 11 miles?
- What does the flat part of the graph mean?
- What is the equation of the line from 0 to 8 minutes?
- What is the equation of the line from 8 minutes onwards?



Topic/Skill	Definition/Tips	Example
1. Place Value	The <b>value</b> of where a <b>digit</b> is within a number.	In 726, the value of the 2 is 20, as it is in the 'tens' column.
2. Place Value Columns	The names of the columns that <b>determine the value of each digit</b> .  The 'ones' column is also known as the 'units' column.	<p>PLACE VALUE CHART</p> 
3. Rounding	To make a number simpler but keep its value close to what it was.  If the <b>digit to the right</b> of the rounding digit is <b>less than 5, round down</b> . If the <b>digit to the right</b> of the rounding digit is <b>5 or more, round up</b> .	<p>74 rounded to the nearest ten is 70, because 74 is closer to 70 than 80.</p> <p>152,879 rounded to the nearest thousand is 153,000.</p>
4. Decimal Place	The <b>position</b> of a digit to the <b>right of a decimal point</b> .	<p>In the number 0.372, the 7 is in the second decimal place.</p> <p>0.372 rounded to two decimal places is 0.37, because the 2 tells us to round down.</p> <p>Careful with money – do not write £27.4, instead write £27.40</p>
5. Significant Figure	The significant figures of a number are the digits which <b>carry meaning</b> (ie. are significant) to the size of the number.  The <b>first significant figure</b> of a number <b>cannot be zero</b> .  In a number with a decimal, trailing zeros are not significant.	<p>In the number 0.00821, the first significant figure is the 8.</p> <p>In the number 2.740, the 0 is not a significant figure.</p> <p>0.00821 rounded to 2 significant figures is 0.0082.</p> <p>19357 rounded to 3 significant figures is 19400. We need to include the two zeros at the end to keep the digits in the same place value columns.</p>
6. Truncation	A method of approximating a decimal number by <b>dropping all decimal places</b> past a certain point <b>without rounding</b> .	3.14159265... can be truncated to 3.1415 (note that if it had been rounded, it would become 3.1416)
7. Error Interval	A <b>range of values</b> that a number could have taken before being rounded or truncated.  An error interval is written using inequalities, with a <b>lower bound</b> and an <b>upper bound</b> .  Note that the lower bound inequality can be 'equal to', but the upper bound cannot be 'equal to'.	<p>0.6 has been rounded to 1 decimal place.</p> <p>The error interval is:</p> $0.55 \leq x < 0.65$ <p>The lower bound is 0.55 The upper bound is 0.65</p>
8. Integer	A <b>whole number</b> that can be positive, negative or zero.	-3, 0, 92



9. Decimal	A number with a <b>decimal point</b> in it. Can be positive or negative.	3.7, 0.94, -24.07
10. Negative Number	A number that is <b>less than zero</b> . Can be decimals.	-8, -2.5
11. Ratio	Ratio compares the size of <b>one part to another part</b> .  Written using the ':' symbol.	<b>3 : 1</b> 
12. Proportion	Proportion compares the size of <b>one part</b> to the size of the <b>whole</b> .  Usually written as a fraction.	In a class with 13 boys and 9 girls, the proportion of boys is $\frac{13}{22}$ and the proportion of girls is $\frac{9}{22}$
13. Simplifying Ratios	<b>Divide</b> all parts of the ratio by a <b>common factor</b> .	5 : 10 = 1 : 2 (divide both by 5) 14 : 21 = 2 : 3 (divide both by 7)
14. Ratios in the form 1 : n or n : 1	<b>Divide</b> both parts of the ratio by one of the numbers to make <b>one part equal 1</b> .	5 : 7 = 1 : $\frac{7}{5}$ in the form 1 : n 5 : 7 = $\frac{5}{7}$ : 1 in the form n : 1
15. Sharing in a Ratio	<b>1. Add</b> the total parts of the ratio. <b>2. Divide</b> the amount to be shared by this value to find the value of one part. <b>3. Multiply</b> this value by each part of the ratio.  Use only if you <b>know the total</b> .	Share £60 in the ratio 3 : 2 : 1.  $3 + 2 + 1 = 6$ $60 \div 6 = 10$ $3 \times 10 = 30, 2 \times 10 = 20, 1 \times 10 = 10$ £30 : £20 : £10

### Try these ...

**7 a** Work out

i  $26.8 + 10$

ii  $26.8 \times 0.01$

iii  $26.8 \times 0.1$

**b** Explain why two of the calculations give the same answer.

**10** Simplify these ratios.

**a** 24 : 120

**b** 20 : 7.5





Topic/Skill	Definition/Tips	Example								
<b>7.1 Quadrilaterals</b>	<p>Classify Quadrilaterals by their geometric properties.</p> <p>Solve problems using side and angle properties of special quadrilaterals.</p>	<p><b>Key point</b> A <b>diagonal</b> is a line that joins two opposite vertices of a shape. When diagonals <b>bisect</b> each other, they cut each other in half. The <b>properties</b> of a shape are facts about its sides, angles, diagonals and symmetry. Here are some of the properties of the special quadrilaterals that you should know.</p> <table><tr><td><b>Square</b> <ul style="list-style-type: none"><li>all sides are equal in length</li><li>opposite sides are parallel</li><li>all angles are 90°</li><li>diagonals bisect each other at 90°</li></ul></td><td><b>Rectangle</b> <ul style="list-style-type: none"><li>opposite sides are equal in length</li><li>opposite sides are parallel</li><li>all angles are 90°</li><li>diagonals bisect each other</li></ul></td></tr><tr><td><b>Rhombus</b> <ul style="list-style-type: none"><li>all sides are equal in length</li><li>opposite sides are parallel</li><li>opposite angles are equal</li><li>diagonals bisect each other at 90°</li></ul></td><td><b>Parallelogram</b> <ul style="list-style-type: none"><li>opposite sides are equal in length</li><li>opposite sides are parallel</li><li>opposite angles are equal</li><li>diagonals bisect each other</li></ul></td></tr><tr><td><b>Kite</b> <ul style="list-style-type: none"><li>2 pairs of sides are equal in length</li><li>no parallel sides</li><li>1 pair of equal angles</li><li>diagonals bisect each other at 90°</li></ul></td><td><b>Trapezium</b> <ul style="list-style-type: none"><li>1 pair of parallel sides</li></ul></td></tr><tr><td></td><td><b>Isosceles trapezium</b> <ul style="list-style-type: none"><li>2 sides are equal in length</li><li>1 pair of parallel sides</li><li>2 pairs of equal angles</li></ul></td></tr></table> <p><b>Worked example</b> In this parallelogram, one of the angles is 55°. Work out the sizes of the other angles. <math>x = 55^\circ</math> (opposite angles of a parallelogram are equal) <math>360 - 55 - 55 = 250^\circ</math> (angles in a quadrilateral add up to 360°) <math>250 \div 2 = 125^\circ</math> (opposite angles of a parallelogram are equal) <math>y = 125^\circ</math> and <math>z = 125^\circ</math></p> <p>Identify equal angles. Write the reasons.</p>	<b>Square</b> <ul style="list-style-type: none"><li>all sides are equal in length</li><li>opposite sides are parallel</li><li>all angles are 90°</li><li>diagonals bisect each other at 90°</li></ul>	<b>Rectangle</b> <ul style="list-style-type: none"><li>opposite sides are equal in length</li><li>opposite sides are parallel</li><li>all angles are 90°</li><li>diagonals bisect each other</li></ul>	<b>Rhombus</b> <ul style="list-style-type: none"><li>all sides are equal in length</li><li>opposite sides are parallel</li><li>opposite angles are equal</li><li>diagonals bisect each other at 90°</li></ul>	<b>Parallelogram</b> <ul style="list-style-type: none"><li>opposite sides are equal in length</li><li>opposite sides are parallel</li><li>opposite angles are equal</li><li>diagonals bisect each other</li></ul>	<b>Kite</b> <ul style="list-style-type: none"><li>2 pairs of sides are equal in length</li><li>no parallel sides</li><li>1 pair of equal angles</li><li>diagonals bisect each other at 90°</li></ul>	<b>Trapezium</b> <ul style="list-style-type: none"><li>1 pair of parallel sides</li></ul>		<b>Isosceles trapezium</b> <ul style="list-style-type: none"><li>2 sides are equal in length</li><li>1 pair of parallel sides</li><li>2 pairs of equal angles</li></ul>
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<b>7.2 Alternate angles and proof</b>	<p>Identify alternate angles on a diagram.</p> <p>Understand proofs of angle facts.</p>	<p><b>Key point</b> When a line crosses two parallel lines it creates a 'Z' shape. Inside the Z shape are <b>alternate angles</b>. Alternate angles are equal. Alternate angles are on different (alternate) sides of the diagonal line.</p> <p><b>Worked example</b> Write the sizes of angles <math>x</math> and <math>y</math>. Give reasons for your answers. <math>x = 72^\circ</math> (alternate angle with <math>72^\circ</math>) <math>y = 180 - 72 = 108^\circ</math> (angles on a straight line add up to 180°)</p>								
<b>7.3 Angles in parallel lines</b>	<p>Identify corresponding angles. Solve problems using properties of angles in parallel and intersecting lines.</p>	<p><b>Key point</b> When a line crosses two parallel lines it creates an 'F' shape. There are <b>corresponding angles</b> on an F shape. Corresponding angles are equal. Corresponding angles are on the same (corresponding) side of the diagonal line.</p> <p><b>Worked example</b> Write the sizes of angles <math>x</math>, <math>y</math> and <math>z</math>. Give reasons for your answers. <math>x = 180 - 105 = 75^\circ</math> (angles on a straight line add up to 180°) <math>y = 105^\circ</math> (corresponding angle with <math>105^\circ</math>) <math>z = 75^\circ</math> (corresponding angle with <math>x</math>)</p>								
<b>7.4 Exterior and Interior angles</b>	<p>Calculate the sum of the interior and exterior angles of a polygon.</p>	<p><b>Key point</b> The interior and exterior angles of a polygon are shown in the diagram.</p> <p>In an <b>irregular polygon</b> sides are not all equal lengths, and angles are not all equal.</p>								



Work out the sizes of interior and exterior angles of a polygon.

Sum of Interior Angles

$(n - 2) \times 180$   
where  $n$  is the number of sides.

Size of Interior Angle in a Regular Polygon

$\frac{(n - 2) \times 180}{n}$

You can also use the formula:  
 **$180 - \text{Size of Exterior Angle}$**

Size of Exterior Angle in a Regular Polygon

$\frac{360}{n}$

You can also use the formula:  
 **$180 - \text{Size of Interior Angle}$**

#### Key point

The angles in a quadrilateral add up to  $360^\circ$ .

$$a + b + c + d = 360^\circ$$



#### Key point 6

The sum of the exterior angles of a regular polygon is always  $360^\circ$ .

### 7.5 Solving geometric problems

Solve geometrical problems

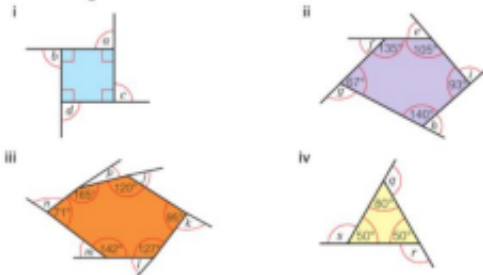
10 For each irregular polygon, work out

- the sum of the interior angles
- the size of the angle marked with a letter.



- 10 a i  $360^\circ$  ii  $x = 163^\circ$   
b i  $540^\circ$  ii  $y = 160^\circ$   
c i  $720^\circ$  ii  $z = 129^\circ$

5 a For each polygon, work out the size of each exterior angle, and then the sum of the exterior angles.



b Reasoning What do you notice about the sum of the exterior angles for each shape?

- 5 a i  $a = b = c = d = 90^\circ$   
sum =  $360^\circ$   
ii  $e = 75^\circ, f = 45^\circ, g = 113^\circ, h = 40^\circ, i = 87^\circ$   
sum =  $360^\circ$   
iii  $j = 60^\circ, k = 85^\circ, l = 53^\circ, m = 38^\circ, n = 109^\circ, p = 15^\circ$   
sum =  $360^\circ$   
iv  $q = 100^\circ, r = s = 130^\circ$   
sum =  $360^\circ$   
b The sum is always the same.



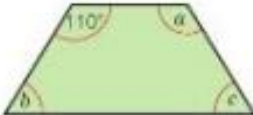
Try these ...

1. Write which quadrilaterals
- |                                 |   |
|---------------------------------|---|
| a have all sides equal          | b have four right angles                  |
| c have two pairs of equal sides | d have exactly one pair of parallel sides |
| e have bisecting diagonals      | f can have four different sized angles.   |

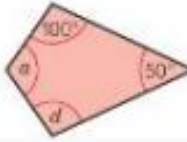
2. In this parallelogram, one of the angles is  $130^\circ$ . Work out the sizes of the other angles.



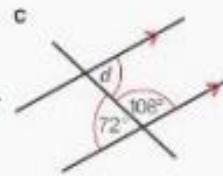
- i Work out the sizes of the angles marked with letters in this isosceles trapezium.



Work out the sizes of the angles marked with letters in this kite.



3. **Reasoning** Write the sizes of the angles marked with letters. Give a reason for each answer.



4. Work out the missing exterior angles for each of these polygons.

