YEAR 9 - REASONING WITH GEOMETRY ...

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Enlargement & Similarity

What do I need to be able to do?

By the end of this unit you should be able to:

- Recognise enlargement and similarity
- Enlarge a shape by a positive SF
- Enlarge a shape from a point
- Enlarge a shape by a fractional SF
- Work out missing sides and angles in a pair of similar shapes.

<u>Keywords</u>

Similar Shapes: shapes of different sizes that have corresponding sides in equal proportion and identical corresponding angles.

Scale Factor: the multiple describing how much a shape has been enlarged

Enlarge: to change the size of a shape (enlargement is not always making a shape bigger)

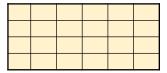
Corresponding: objects (or sides) that appear in the same place in two similar situations.

Image: the picture or visual representation of the shape

Recognise enlargement & similarity

Shapes are similar if all pairs of corresponding sides are in the same ratio

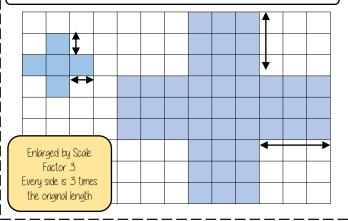
These shapes are similar because all sides are increased by the same ratio



Enlargements are similar shapes with a ratio other than I

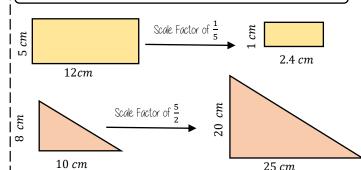
Enlarge by a positive scale factor

With a scale factor larger than 1 it makes the shape **bigger**



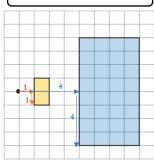
Positive fractional scale factor

With a scale factor between 0 and 1 it makes the shape **smaller**



Enlarge a shape from a point

Scaled distances method



Multiply the distance from the centre of corresponding vertices by the scale

factor along the ray

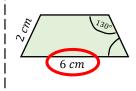
Raus method

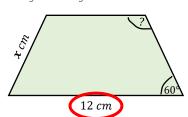
Scale the distance between the point of enlargement and each corresponding

<u>Calculations in similar shapes</u>

Don't forget that properties of shapes don't change with enlargements or in similar shapes

The two trapezium are similar find the missing side and angle





Corresponding sides identify the scale factor

$$\frac{12}{6} = 2$$

Scale Factor = 2

Calculate the missing side

Length (corresponding side) x scale factor

 $2cm \times 2$

x = 4cm

Enlargement does not change angle size

<u>Calculate the missing angle</u> Corresponding angles remain the same 130°

YEAR 9 - REASONING WITH GEOMETRY

Solving ratio & proportion problems

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What do I need to be able to do?

By the end of this unit you should be able to:

- Solve problems with direct proportion
- Use conversion graphs
- Solve problems with inverse proportion
- Solve ratio problems
- Solve 'best buy' problems

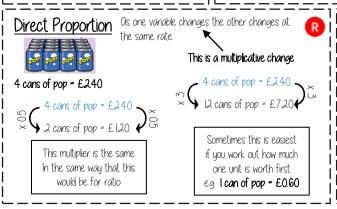
!! <u>Keywords</u>

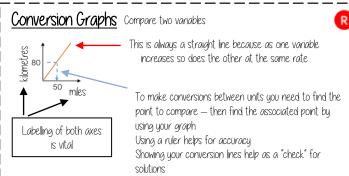
Proportion: a comparison between two numbers

Ratio: a ratio shows the relative size of two variables

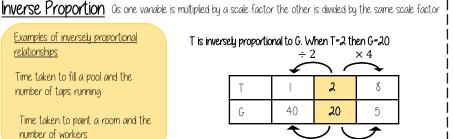
Direct proportion: as one variable is multiplied by a scale factor the other variable is multiplied by the same scale factor.

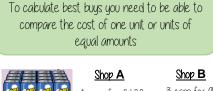
Inverse proportion:: as one variable is multiplied by a scale factor the other is divided by the same scale factor.





Best Buys



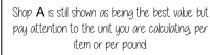


Have a directly proportional relationship

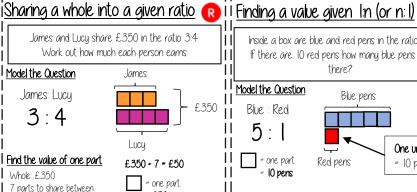


Shop Ais the best value as it is lp cheaper per can of pop





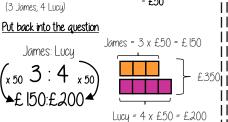
Best value is the most product for the lowest price per unit

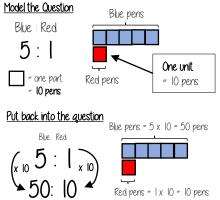


(3 James, 4 Lucy)

James: Lucu

►£ 150:£200





There are 50 Blue Pens

Inside a box are blue and red pens in the ratio 5:1

If there are 10 red pens how many blue pens are there?

YEAR 9 - REASONING WITH GEOMETRY.

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Rates

What do I need to be able to do?

By the end of this unit you should be able to:

- Solve speed, distance, time questions
- Use distance time graphs
- Solve density, mass, volume problems
- Solve flow problems
- Use flow graphs
- Interpret rates of change and their units

<u>Keywords</u>

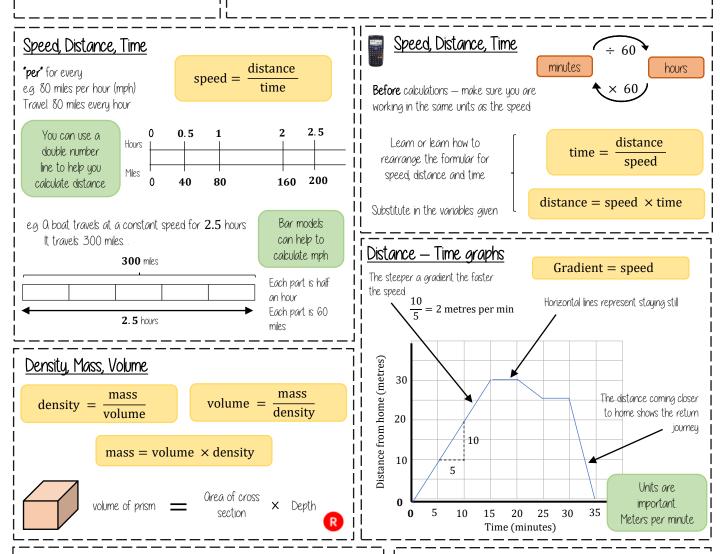
Convert: change

Mass: a measure of how much matter is in an object. Commonly measured by weight.

Origin: the coordinate (0, 0)

Volume: the amount of 3D space a shape takes up

Substitute: putting numbers where letters are — replacing numbers into a formula



Flow problems & graphs

This will fill at a constant rate, then as the space decreases it will speed up and the neck of the bottle fill at a faster constant speed

The cylinder will fill at a constant speed

Units are important Ensure any volume calculations are the same unit as the rate of flow

Rates of change & units Common rates of change relationships Revisit your conversions between units of length and capacity Exchange rates: euros per pounds Density: mass per volume kilometres kilometres

YEAR 9 - REPRESENTATIONS.

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Probability

What do I need to be able to do?

By the end of this unit you should be able to:

- Find single event probability
- Find relative frequency
- Find expected outcomes
- Find independent events
- Use diagrams to work out probabilities

<u>Keywords</u>

Probability: the chance that something will happen

Relative Frequency: how often something happens divided by the outcomes

Independent: an event that is not effected by any other events.

Chance: the likelihood of a particular outcome.

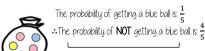
Event: the outcome of a probability — a set of possible outcomes.

Biased: a built in error that makes all values wrong by a certain amount.

The probability scale 0 or 0% 1 or 100% $0.5, \frac{1}{2}$ or 50%The more likely an event the further up the probability it will be in comparison to another event ★(It will have a probability closer to 1) There are 2 pink and 2 There are 5 possible outcomes yellow balls, so So 5 intervals on this scale, each theu have the interval value is 🖠 ame probabilitu

🔃 I Single event probabilitu

Probability is always a value between 0 and 1



The sum of the probabilities is 1

The table shows the probability of selecting a type of chocolate

Dark	Milk	White
0.15	0.35	

P(white chocolate) = 1 - 0.15 - 0.35



Relative Frequency

Frequency of event Total number of outcomes

Remember to calculate or identify the overall number of outcomes!

Colour	Frequency	Relative Frequency
Green	6	0.3
Yellow	12	0.6
Blue	2	0.1
	20	

Relative frequency can be used to find expected

e.g. Use the relative probability to find the expected outcome for green if there are 100 selections.

Relative frequency x Number of times $0.3 \times 100 = 30$

Expected outcomes

Expected outcomes are estimations. It is a long term average rather than a prediction.

Dark	Milk	White	
0.15	0.35	0.5	

The sum of the probabilities is $oldsymbol{1}$

On experiment is carried out 400 Show that dark chocolate is expected

to be selected 60 times

 $0.15 \times 400 = 60$

Independent events



The rolling of one dice has no impact on the rolling of the other. The individual probabilities should be calculated separately.

Probability of event 1 × Probability of event 2



$$P(5) = \frac{1}{6}$$

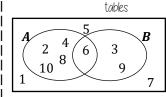
$$P(5) = \frac{1}{6}$$
 $P(R) = \frac{1}{4}$

Find the probability of getting a 5 and

$$P(5 \text{ and } R) = \frac{1}{6} \times \frac{1}{4} = \frac{1}{24}$$

Using diagrams Recap Venn diagrams, Sample space diagrams and Two-way

Ш



	Car		Walk	Total	
Boys	15	24	14	53	
Girls	6	20	21	47	
Total	21	44	35	100	

NO.

The possible outcomes from rolling a d						2
1	2	3	4	5	6	
111	011	0.11	4.11	611	CII	

20 00 00 00 00 00 00 00 00 00 00 00 00 0			1	2	3	4	5	6
ne possible wa from tossing a		Н	ľH	2,H	3,H	4,H	5,H	6,H
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YFAR 9 - REPRESENTATIONS

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Algebraic Representation

What do I need to be able to do?

By the end of this unit you should be able to:

- Draw quadratic graphs
- Interpret quadratic graphs
- Interpret other graphs including reciprocals
- Represent inequalities

Keywords

Quadratic: a curved graph with the highest power being 2. Square power.

Inequality: makes a non equal comparison between two numbers

Reciprocal: a reciprocal is 1 divided by the number

Cubic: a curved graph with the highest power being 3. Cubic power.

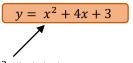
Origin: the coordinate (0, 0)

Parabola: a 'u' shaped curve that has mirror symmetry

Intersection with

the γ axis

Quadratic Graphs

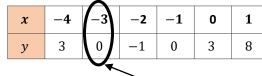


If x^2 is the highest power in your equation then you have a quadratic graph.

It will have a parabola shape



Quadratic graphs are always symmetrical with the turning point in the middle



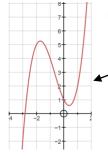
Coordinate pairs for plotting (-3,0)

Plot all of the coordinate pairs and join the points with a curve (freehand)

Interpret other graphs

Cubic Graphs

$$y = x^3 + 2x^2 - 2x + 1$$



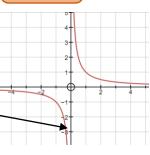
If x^3 is the highest power in your equation then you have a <u>cubic graph</u>

> Reciprocal graphs never touch the ν axis.

This is because x cannot be 0This is an asymptote



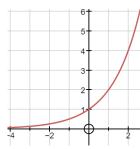




Exponential Graphs



Exponential graphs have a power of x

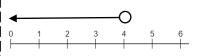


Represent Inequalities

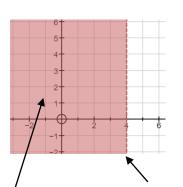
Multiple methods of representing inequalities



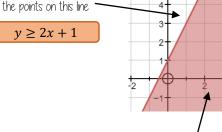
Oll values are less than 4



The shaded area indicates all possible values of x



The solid line shows that the inequality includes all



The shaded area indicates all possible solutions to this inequality

The dotted line shows that the inequality does not include these points