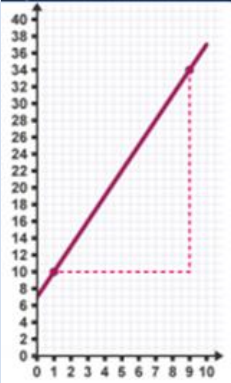
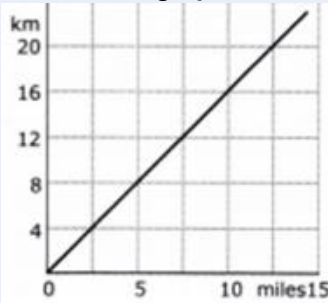
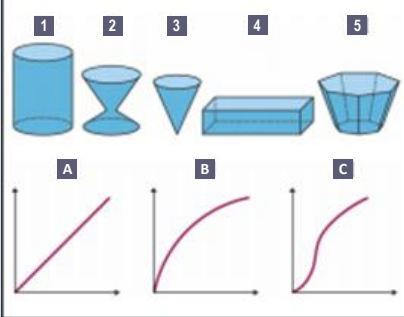
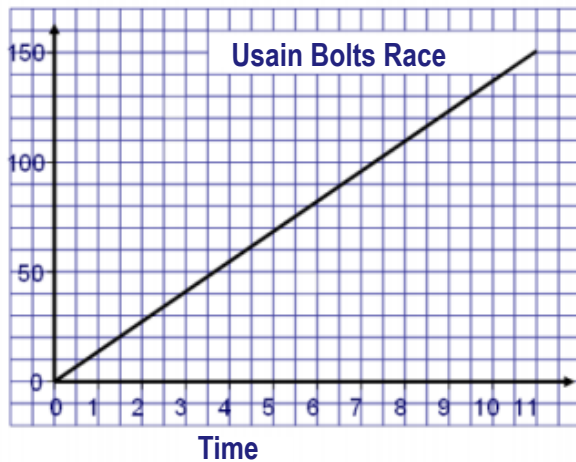


	Topic/Skill	Definition/Tips	Example
1.	Real life graphs	<p>Graphs that are supposed to model some real-life situation.</p> <p>The actual meaning of the values depends on the labels and units on each axis.</p> <p>The <b>gradient</b> might have a contextual meaning. The <b>y-intercept</b> might have a contextual meaning.</p> <p>The <b>area</b> under the graph might have a contextual meaning.</p>	 <p>A graph showing the cost of hiring a ladder for various numbers of days.</p> <p>The gradient shows the cost per day. Its costs £3/day to hire the ladder.</p> <p>The y-intercept shows the additional cost/deposit/charged (something not linked to how long the ladder is hired for). The additional cost is £7</p>
2.	Conversion graph	<p>A line graph to <b>convert one unit to another</b>.</p> <p>Can be used to convert units (e.g. miles and kilometres ) or currencies (\$ and £)</p> <p>Find the value you know on one axis, read up/across to the conversion line and read the equivalent value from the other axis.</p>	<p>Conversion graph ↔ miles kilometres</p>  <p>8km = 5 miles</p>
3.	Depth of water in containers	<p>Graphs can be used to show how the depth of water changes as different shaped containers are filled with water at a constant rate.</p>	

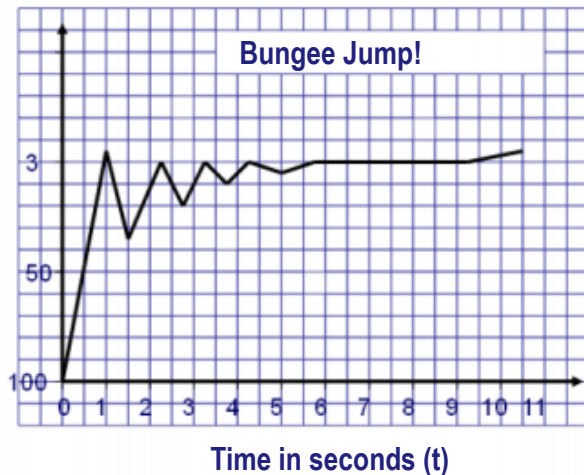
**Try These**

Distance  
(metres)



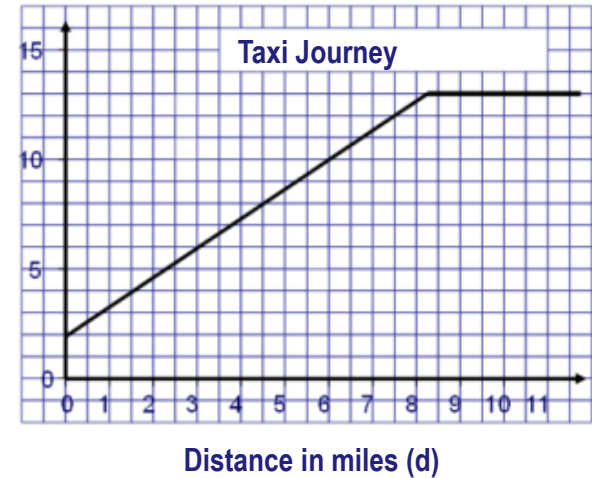
- How far has he run after 4.5 seconds?
- How long has it taken Usain to run 130 metres?
- How far has he run after 8 seconds?
- Why does the line go through the origin?

Distance  
to from  
the floor  
in metres  
(h)




- How high is the bungee jump?
- Why does the graph zig-zag?
- How long is the person falling for until they begin to bounce back up?
- Why does the person stop at 3 metres and 0?
- How long is the person not bouncing but still upside down for?

Taxi Fare  
in £ (f)



- Why does the taxi fare not go through the origin?
- How much does it cost to travel 6 miles?
- How far can I travel if I only have £10 in my pocket?
- What does the journey cost after 9 miles? And after 11 miles?
- What does the flat part of the graph mean?
- What is the equation of the line from 0 to 8 minutes?
- What is the equation of the line from 8 minutes onwards?

	Topic/Skill	Definition/Tips	Example
1.	Place Value	The value of where a <b>digit</b> is within a number.	In 726, the value of the 2 is 20, as it is in the 'tens' column
2.	Place Value Columns	The names of the columns that <b>determine the value of each digit</b> . The 'ones' column is also known as the 'units' column.	<p><b>PLACE VALUE CHART</b></p>
3.	Rounding	To make a number simpler but keep its value close to what it was. If the <b>digit to the right</b> of the rounding digit is <b>less than 5, round down</b> . If the <b>digit to the right</b> of the rounding digit is <b>5 or more, round up</b> .	74 rounded to the nearest ten is 70, because 74 is closer to 70 than 80. 152,879 rounded to the nearest thousand is 153,000
4.	Decimal Place	The <b>position</b> of a digit to the <b>right of a decimal point</b> .	In the number 0.372, the 7 is in the second decimal place. 0.372 rounded to two decimal places is 0.37, because the 2 tells us to round down. Careful with money – do not write £27.4, instead write £27.40
5.	Significant Figure	The significant figures of a number are the digits which <b>carry meaning</b> (i.e. are significant) to the size of the number. The <b>first significant figures</b> of a number <b>cannot be zero</b> . In a number with a decimal, trailing zeros are not significant.	In the number 0.00821, the first significant figure is the 8. In the number 2.740 the 0 is not a significant figure. 0.00821 rounded to 2 significant figures is 0.0082 19357 rounded to 3 significant figures is 19400. we need to include the two zeros at the end to keep the digits in the same place value columns.
6.	Truncation	A method of approximating a decimal number by <b>dropping all decimal</b> places past a certain point <b>without rounding</b> .	3.14159265... can be truncated to 3.1415 (note that if it had been rounded, it would become 3.1415)
7.	Error Interval	A <b>range of values</b> that a number could have taken before being rounded or truncated. An error interval is written using inequalities, with a <b>lower bound</b> and an <b>upper bound</b> . Note that the lower bound inequality can be 'equal to', but the upper bound cannot be 'equal to'.	0.6 has been rounded to 1 decimal place. The error interval is: $0.55 \leq x < 0.65$ The lower bound is 0.55 The upper bound is 0.65
8.	Integer	A <b>whole number</b> that can be positive, negative or zero.	-3, 0, 92

	Topic/Skill	Definition/Tips	Example
9.	Decimal	A number with a <b>decimal point</b> in it. Can be positive or negative	3.7, 0.94, -24.07
10.	Negative number	A number that is <b>less than zero</b> . Can be decimals	-8, -2.5
11.	Ratio	Ratio compares the size of <b>one part</b> to <b>another part</b> . Written using the ' : ' symbol.	3:1 
12.	Proportion	Proportion compares the size of <b>one part</b> to the size of the <b>whole</b> . Usually written as a fraction	In a class with 13 boys and 9 girls, the proportion of boys is $\frac{13}{22}$ is and the proportion of girls is $\frac{9}{22}$
13.	Simplifying Ratios	<b>Divide</b> all parts of the ratio by a <b>common factor</b>	5 : 10 = 1 : 2 (divide both by 5) 14 : 21 = 2 : 3 (divide both by 7)
14.	Ratios in the form 1 : n or n : 1	<b>Divide</b> both part of the ratio by one of the numbers to make <b>one part equal 1</b>	5 : 7 = 1 : $\frac{7}{5}$ in the form 1 : n 5 : 7 = $\frac{5}{7}$ : 1 in the form n : 1
15.	Sharing in a Ratio	<ol style="list-style-type: none"> <li><b>Add</b> the total part of the ratio</li> <li><b>Divide</b> the amount to be shared by this value to find the value of one part</li> <li><b>Multiply</b> this value by each part of the ratio</li> </ol> Use only if you <b>know the total</b>	Share £60 in the ratio 3 : 2 : 1 $3 + 2 + 1 = 6$ $60 \div 6 = 10$ $3 \times 10 = 30, 2 \times 10 = 20, 1 \times 10 = 10$ £30 : £20 : £10

**Try these ...**

1a) Work out


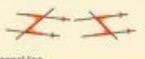
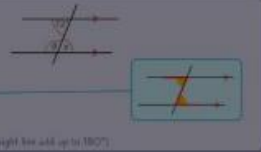

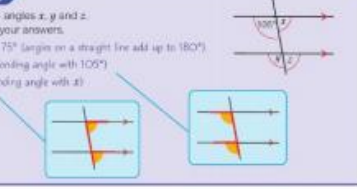
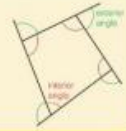
- $26.8 \div 10$
- $26.8 \times 0.01$
- $26.8 \times 0.1$

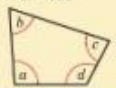




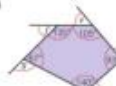
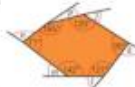

b) Explain why two of the calculations give the same answer

Simplify these ratios

2 a) 24 : 120

b) 20 : 7.5

Topic/Skill	Definition/Tips	Example								
7.1 Quadrilaterals	<p>Classify Quadrilaterals by their geometric properties.</p> <p>Solve problems using side and angle properties of special quadrilaterals.</p>	<p><b>Key point</b> A diagonal is a line that joins two opposite vertices of a shape. When diagonals bisect each other, they cut each other in half.</p> <p>The properties of a shape are facts about its sides, angles, diagonals and symmetry. Here are some of the properties of the special quadrilaterals that you should know.</p> <table border="1"> <tr> <td> <p><b>Square</b></p> <ul style="list-style-type: none"> <li>all sides are equal in length</li> <li>opposite sides are parallel</li> <li>all angles are <math>90^\circ</math></li> <li>diagonals bisect each other at <math>90^\circ</math></li> </ul> </td> <td> <p><b>Rectangle</b></p> <ul style="list-style-type: none"> <li>opposite sides are equal in length</li> <li>opposite sides are parallel</li> <li>all angles are <math>90^\circ</math></li> <li>diagonals bisect each other</li> </ul> </td> </tr> <tr> <td> <p><b>Rhombus</b></p> <ul style="list-style-type: none"> <li>all sides are equal in length</li> <li>opposite sides are parallel</li> <li>opposite angles are equal</li> <li>diagonals bisect each other at <math>90^\circ</math></li> </ul> </td> <td> <p><b>Parallelogram</b></p> <ul style="list-style-type: none"> <li>opposite sides are equal in length</li> <li>opposite sides are parallel</li> <li>opposite angles are equal</li> <li>diagonals bisect each other</li> </ul> </td> </tr> <tr> <td> <p><b>Kite</b></p> <ul style="list-style-type: none"> <li>2 pairs of sides are equal in length</li> <li>no parallel sides</li> <li>1 pair of equal angles</li> <li>diagonals bisect each other at <math>90^\circ</math></li> </ul> </td> <td> <p><b>Trapezium</b></p> <ul style="list-style-type: none"> <li>1 pair of parallel sides</li> </ul> </td> </tr> <tr> <td> <p><b>Isosceles trapezium</b></p> <ul style="list-style-type: none"> <li>2 sides are equal in length</li> <li>1 pair of parallel sides</li> <li>2 pairs of equal angles</li> </ul> </td> <td></td> </tr> </table> <p><b>Worked example</b></p> <p>In this parallelogram, one of the angles is <math>55^\circ</math>. Work out the sizes of the other angles.</p> <p><math>x = 55^\circ</math> (opposite angles of a parallelogram are equal)</p> <p><math>360 - 55 - 55 = 250^\circ</math> (angles in a quadrilateral add up to <math>360^\circ</math>)</p> <p><math>250 \div 2 = 125^\circ</math> (opposite angles of a parallelogram are equal)</p> <p><math>y = 125^\circ</math> and <math>z = 125^\circ</math></p> <p>Identify equal angles. Write the reason.</p> 	<p><b>Square</b></p> <ul style="list-style-type: none"> <li>all sides are equal in length</li> <li>opposite sides are parallel</li> <li>all angles are <math>90^\circ</math></li> <li>diagonals bisect each other at <math>90^\circ</math></li> </ul>	<p><b>Rectangle</b></p> <ul style="list-style-type: none"> <li>opposite sides are equal in length</li> <li>opposite sides are parallel</li> <li>all angles are <math>90^\circ</math></li> <li>diagonals bisect each other</li> </ul>	<p><b>Rhombus</b></p> <ul style="list-style-type: none"> <li>all sides are equal in length</li> <li>opposite sides are parallel</li> <li>opposite angles are equal</li> <li>diagonals bisect each other at <math>90^\circ</math></li> </ul>	<p><b>Parallelogram</b></p> <ul style="list-style-type: none"> <li>opposite sides are equal in length</li> <li>opposite sides are parallel</li> <li>opposite angles are equal</li> <li>diagonals bisect each other</li> </ul>	<p><b>Kite</b></p> <ul style="list-style-type: none"> <li>2 pairs of sides are equal in length</li> <li>no parallel sides</li> <li>1 pair of equal angles</li> <li>diagonals bisect each other at <math>90^\circ</math></li> </ul>	<p><b>Trapezium</b></p> <ul style="list-style-type: none"> <li>1 pair of parallel sides</li> </ul>	<p><b>Isosceles trapezium</b></p> <ul style="list-style-type: none"> <li>2 sides are equal in length</li> <li>1 pair of parallel sides</li> <li>2 pairs of equal angles</li> </ul>	
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7.2 Alternate angles and proof	<p>Identify alternate angles on a diagram.</p> <p>Understand proofs of angle facts.</p>	<p><b>Key point</b> When a line crosses two parallel lines it creates a 'Z' shape. Inside the Z shape are <b>alternate angles</b>. Alternate angles are equal. Alternate angles are on different (alternate) sides of the diagonal line.</p>  <p><b>Worked example</b></p> <p>Write the sizes of angles <math>x</math> and <math>y</math>. Give reasons for your answers.</p> <p><math>x = 72^\circ</math> (alternate angle with <math>72^\circ</math>)</p> <p><math>y = 180 - 72 = 108^\circ</math> (angles on a straight line add up to <math>180^\circ</math>)</p> 								
7.3 Angles in parallel lines	<p>Identify corresponding angles.</p> <p>Solve problems using properties of angles in parallel and intersecting lines.</p>	<p><b>Key point</b> When a line crosses two parallel lines it creates an 'F' shape. There are <b>corresponding angles</b> on an F shape. Corresponding angles are equal. Corresponding angles are on the same (corresponding) side of the diagonal line.</p>  <p><b>Worked example</b></p> <p>Write the sizes of angles <math>x</math>, <math>y</math> and <math>z</math>. Give reasons for your answers.</p> <p><math>x = 180 - 105 = 75^\circ</math> (angles on a straight line add up to <math>180^\circ</math>)</p> <p><math>y = 105^\circ</math> (corresponding angle with <math>105^\circ</math>)</p> <p><math>z = 75^\circ</math> (corresponding angle with <math>x</math>)</p> 								
7.4 Exterior and Interior angles	<p>Calculate the sum of the interior and exterior angles of a polygon.</p>	<p><b>Key point</b> The interior and exterior angles of a polygon are shown in the diagram.</p> <p>In an <b>irregular polygon</b> sides are not all equal lengths, and angles are not all equal.</p> 								

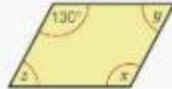
	<p>Work out the sizes of interior and exterior angles of a polygon.</p>	<table border="1"> <tr> <td data-bbox="1014 37 1178 121">Sum of Interior Angles</td> <td data-bbox="1178 37 1526 121"> <math>(n - 2) \times 180</math> where <math>n</math> is the number of sides.                 </td> </tr> <tr> <td data-bbox="1014 121 1178 221">Size of Interior Angle in a Regular Polygon</td> <td data-bbox="1178 121 1526 221"> <math display="block">\frac{(n - 2) \times 180}{n}</math> <p>You can also use the formula: <b><math>180 - \text{Size of Exterior Angle}</math></b></p> </td> </tr> <tr> <td data-bbox="1014 221 1178 321">Size of Exterior Angle in a Regular Polygon</td> <td data-bbox="1178 221 1526 321"> <math display="block">\frac{360}{n}</math> <p>You can also use the formula: <b><math>180 - \text{Size of Interior Angle}</math></b></p> </td> </tr> </table> <div data-bbox="1023 349 1294 549" style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p><b>Key point</b></p> <p>The angles in a quadrilateral add up to <math>360^\circ</math>.</p> <math display="block">a + b + c + d = 360^\circ</math>  </div> <div data-bbox="1023 549 1516 592" style="border: 1px solid black; padding: 5px; margin-top: 5px;"> <p><b>Key point 6</b></p> <p>The sum of the exterior angles of a regular polygon is always <math>360^\circ</math>.</p> </div>	Sum of Interior Angles	$(n - 2) \times 180$ where $n$ is the number of sides.	Size of Interior Angle in a Regular Polygon	$\frac{(n - 2) \times 180}{n}$ <p>You can also use the formula: <b><math>180 - \text{Size of Exterior Angle}</math></b></p>	Size of Exterior Angle in a Regular Polygon	$\frac{360}{n}$ <p>You can also use the formula: <b><math>180 - \text{Size of Interior Angle}</math></b></p>
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Size of Exterior Angle in a Regular Polygon	$\frac{360}{n}$ <p>You can also use the formula: <b><math>180 - \text{Size of Interior Angle}</math></b></p>							
<p><b>7.5 Solving geometric problems</b></p>	<p>Solve geometrical problems</p>	<p>10 For each irregular polygon, work out</p> <ol style="list-style-type: none"> <li>the sum of the interior angles</li> <li>the size of the angle marked with a letter.</li> </ol> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div data-bbox="1052 692 1188 778"> <p>a</p>  </div> <div data-bbox="1207 692 1342 778"> <p>b</p>  </div> <div data-bbox="1362 692 1497 778"> <p>c</p>  </div> </div> <div style="margin-top: 20px;"> <p>10 a i <math>360^\circ</math>    ii <math>x = 103^\circ</math>              b i <math>540^\circ</math>    ii <math>g = 100^\circ</math>              c i <math>720^\circ</math>    ii <math>z = 128^\circ</math></p> </div> <p>5 a For each polygon, work out the size of each exterior angle, and then the sum of the exterior angles.</p> <div style="display: flex; justify-content: space-around;"> <div data-bbox="1062 963 1178 1063"> <p>i</p>  </div> <div data-bbox="1284 963 1420 1063"> <p>ii</p>  </div> </div> <div style="display: flex; justify-content: space-around; margin-top: 20px;"> <div data-bbox="1062 1078 1217 1178"> <p>iii</p>  </div> <div data-bbox="1284 1078 1400 1178"> <p>iv</p>  </div> </div> <p><b>b Reasoning</b> What do you notice about the sum of the exterior angles for each shape?</p> <p>5 a i <math>a = b = c = d = 90^\circ</math> sum = <math>360^\circ</math>              ii <math>e = 75^\circ, f = 45^\circ, g = 113^\circ, h = 40^\circ, i = 87^\circ</math> sum = <math>360^\circ</math>              iii <math>j = 60^\circ, k = 65^\circ, l = 53^\circ, m = 38^\circ, n = 109^\circ, p = 15^\circ</math> sum = <math>360^\circ</math>              iv <math>q = 100^\circ, r = s = 130^\circ</math> sum = <math>360^\circ</math></p> <p>b The sum is always the same.</p>						



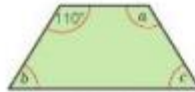
Try these ...

1. Write which quadrilaterals
  - a have all sides equal
  - b have four right angles
  - c have two pairs of equal sides
  - d have exactly one pair of parallel sides
  - e have bisecting diagonals
  - f can have four different sized angles.

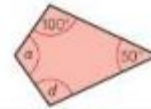
2. In this parallelogram, one of the angles is  $130^\circ$ . Work out the sizes of the other angles.



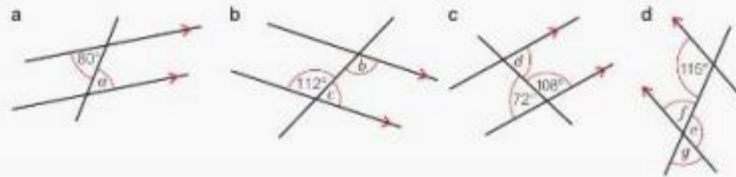
- i Work out the sizes of the angles marked with letters in this isosceles trapezium.



Work out the sizes of the angles marked with letters in this kite.



3. **Reasoning** Write the sizes of the angles marked with letters. Give a reason for each answer.



4. Work out the missing exterior angles for each of these polygons.

