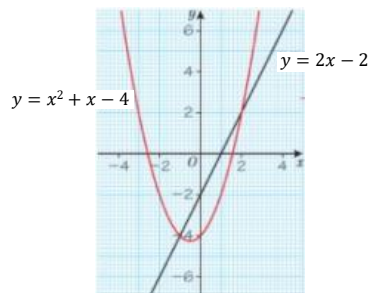


Quadratic Graphs

[V180](#) [V181](#) [V276c](#) [VCubic](#)

Solving Simultaneous Equations



The solutions are:
 $x = 2, y = 2$ and $x = -1, y = -4$

The lowest or highest point of the parabola, where the graph turns, is called the **turning point**.
The turning point is either a minimum or a maximum point
The x-values where the graph intersects the x-axis are the solutions, or **roots** of the equation $y=0$

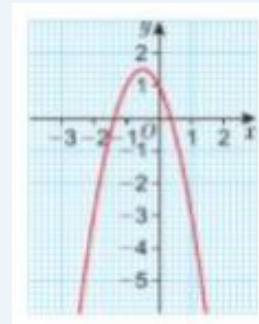


When a quadratic is written in completed square form $y=a(x+b)^2+c$ the coordinate of the turning point is $(-b,c)$

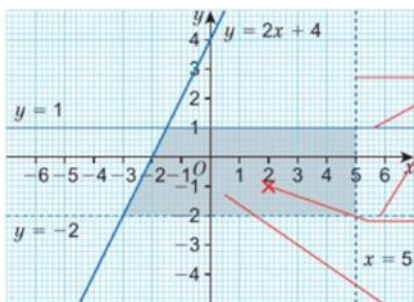
The quadratic equation $ax^2+bx+c=0$ is said to have no real roots if its graph does not cross the x-axis. If its graph just touches the x-axis, the equation has one repeated root.

To sketch a quadratic function

- Calculate the solutions to the equation ' $y=0$ ' (points of intersection with the x-axis)
- Calculate the point at which the graph crosses the y-axis
- Find the coordinates of the turning point and whether it is a maximum or minimum



On a coordinate grid, shade the region that satisfies the inequalities $x < 5, y \leq 2x+4, y \leq 1$ and $y > -2$



Inequality Graphs

Draw dotted lines $x = 5$ and $y = -2$
Draw solid lines $y = 2x + 4, y = 1$

Test a point. For $(2, -1)$
 $y \leq 1$ and $y > -2$: the y-coordinate is -1
 $x < 5$: the x-coordinate is 2
 $2x + 4 = 8$: y-coordinate ≤ 8

Shade the required region.

Cubic Graphs

A **cubic** function is one whose highest power of x is x^3 .
It is written in the form $y=ax^3+bx^2+cx+d$

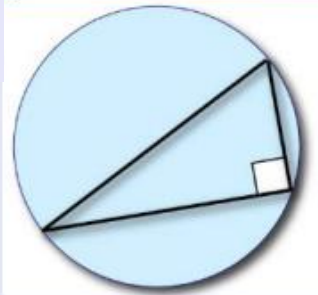
When $a > 0$ the function looks like When $a < 0$ the function looks like



The graph intersects the y-axis at the point $y=d$
The graph's roots can be found by finding the values of x for which $y=0$

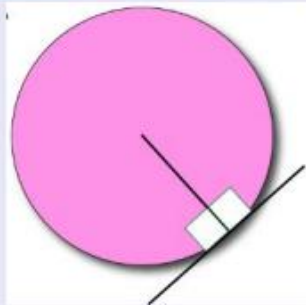
Unit 16 Higher Circle Theorems

V64 V65



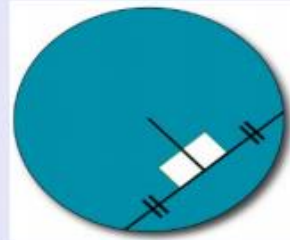
The angle in a semicircle is a right angle.

V65a



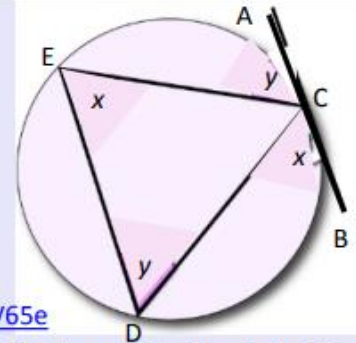
The angle between a **tangent** and **radius** is a right angle.

V65f



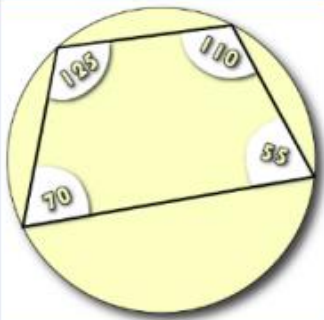
A **chord** is a straight line connecting two points on a circle.

The **perpendicular** from the centre of the circle to a chord **bisects** the chord and the line drawn from the centre of the circle to the **midpoint** of a chord is at right angles to the chord.



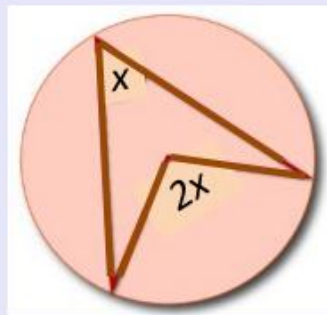
V65e

AB is a tangent to the circle. CD, DE and CE are **chords**. Angle ECA is the angle between the **tangent** and the chord in one segment. The other **segment** has angle CDE. This is the **alternate segment**. The angle between the chord and tangent is equal to the angle in the alternate segment.



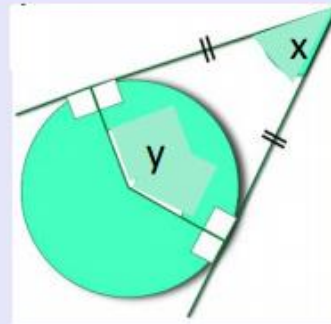
A cyclic quadrilateral with all four vertices on the circumference of the circle. Opposite angles add up to 180° .

V65d

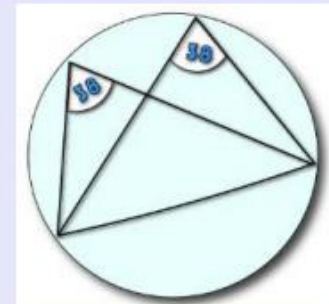


The angle at the centre of a circle is twice the angle at the circumference when both are subtended by the same arc.

V65b



Tangents drawn from a point outside the circle are equal in length.
 $x + y = 180$



Angles in the same segment and standing on the same chord are always equal.

V65c